Statistics and data types

Statistics is the collection, organisation, presentation, analysis and interpretation of data.

Data is a collection of information which may include facts, numbers, measurements or other information.

Data may be gathered by observation, questioning or measurement and is often organised in graphs or charts for statistical analysis.

Types of data

- **Qualitative data**: Describes qualities, characteristics or categories.
- **Quantitative data**: Data where quantities can be counted or measured.
- **Discrete data**: Data that is counted e.g. days in the week. (finite values)
- **Continuous data**: Data that is measured e.g. temperature. (infinite values)

**Leisure Activities Popularity**

<table>
<thead>
<tr>
<th>Leisure Categories</th>
<th>Eating out</th>
<th>Shopping</th>
<th>Phoning friends</th>
<th>Listening to music</th>
<th>TV viewing</th>
<th>Playing sport</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of people</td>
<td>70</td>
<td>60</td>
<td>50</td>
<td>40</td>
<td>30</td>
<td>20</td>
</tr>
</tbody>
</table>

**Daily Temperature Graph**

- **Discrete data**: Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday
- **Continuous data**: Temperature range from -20° to 50°

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Population and sample

In statistics, the population is the whole set of individuals, items or data from which a statistical sample is drawn.

A sample is a selected part of the population.

When a population is too big to gather data from, data is collected from a manageable sample instead.

Oceanarium

population

- sea turtles
- dolphins
- starfish
- squid

fish

seals

crabs

sample

population ... whole group
sample ... part of the group

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Tally, score and frequency

From: A Maths Dictionary for Kids by Jenny Eather at www.amathsdictionaryforkids.com

tally
  • using marks to record counting.
  • count by 5's to get the total

score
  • numerical value.
  • any kind of measurement or count.

frequency
  • the number of times a particular item appears in a set of data.

Oceanarium - Frequency Table

A survey was done at schools close to the Oceanarium to see how many classes had been sent to see the exhibits within the last year.

<table>
<thead>
<tr>
<th>score</th>
<th>tally</th>
<th>frequency (f)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>I</td>
<td>4</td>
</tr>
<tr>
<td>2</td>
<td>II</td>
<td>5</td>
</tr>
<tr>
<td>3</td>
<td>III</td>
<td>6</td>
</tr>
<tr>
<td>4</td>
<td>IIII</td>
<td>10</td>
</tr>
<tr>
<td>5</td>
<td>III</td>
<td>3</td>
</tr>
<tr>
<td>6</td>
<td>II</td>
<td>2</td>
</tr>
</tbody>
</table>

Most schools had a score of 4 class visits.
Types of graphs

A graph is a visual diagram used to represent data values.

There are many types of graphs.

Examples

Pie Graph

<table>
<thead>
<tr>
<th>Percentage</th>
<th>Animal</th>
</tr>
</thead>
<tbody>
<tr>
<td>24%</td>
<td>dolphins</td>
</tr>
<tr>
<td>20%</td>
<td>seals</td>
</tr>
<tr>
<td>16%</td>
<td>crabs</td>
</tr>
<tr>
<td>10%</td>
<td>sharks</td>
</tr>
<tr>
<td>30%</td>
<td></td>
</tr>
</tbody>
</table>

Picture Graph, Pictogram

<table>
<thead>
<tr>
<th>Animal</th>
</tr>
</thead>
<tbody>
<tr>
<td>dolphins</td>
</tr>
<tr>
<td>seals</td>
</tr>
<tr>
<td>crabs</td>
</tr>
<tr>
<td>sharks</td>
</tr>
</tbody>
</table>

Divided Bar Graph

<table>
<thead>
<tr>
<th>Percentage</th>
<th>Animal</th>
</tr>
</thead>
<tbody>
<tr>
<td>20%</td>
<td>crabs</td>
</tr>
<tr>
<td>30%</td>
<td>dolphins</td>
</tr>
<tr>
<td>40%</td>
<td>sharks</td>
</tr>
<tr>
<td>10%</td>
<td>turtles</td>
</tr>
</tbody>
</table>

Horizontal Bar Graph

- dolphins
- seals
- crabs
- sharks

Line Graph

- dolphins
- seals
- crabs
- sharks
A bar graph or bar chart is a commonly used graph for organising and displaying data. Bars are used to show quantities or numbers so they can be easily compared.

Oceanarium - numbers of marine creatures.

Bars may be vertical or horizontal.
A box plot is a diagram or graph using a number line to show the distribution of a set of data. It displays the median, upper and lower quartiles, and the maximum and minimum values of the data.

- the box shows the interquartile range.
- a line in the box marks the median.
- the ‘whiskers’ are lines running from the box to the maximum and minimum values.

- the lower quartile - median of the lower half of the scores.
- the upper quartile - median of the upper half of the scores.

**EXAMPLE:** 60 60 40 74 63 65 88 41 42 57 30 58 66 66 68

1. Arrange the values in ascending order.
   30 40 41 42 57 58 60 60 63 65 66 66 68 74 88
2. Identify the **median** (the value in the middle).
   30 40 41 42 57 58 60 60 63 65 66 66 68 74 88
3. Identify the **lower quartile** (median of the lower half) and the **upper quartile** (median of the upper half).
   30 40 41 42 57 58 60 60 63 65 66 66 68 74 88
4. Draw a box - from the lower to the upper quartile.
5. Draw a line in the box to show the median.
6. Draw the whiskers - to the minimum and maximum.

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A dot plot uses a number line long enough to encompass all numbers in the sample, showing a dot over the position corresponding to each number.

If more than one dot falls in the same position, they are stacked up.

A dot plot of spending patterns.

The amount spent by members of a tour group visiting the Oceanarium.
A conversion graph is a line graph used to convert one unit to another.

**EXAMPLE:** kilometres ... miles conversion

Read across and down: 150 km = 93 miles.

**Whale Watching**
Calculating distances to keep international tourists informed.
Cumulative frequency graph

A cumulative frequency graph is a graph plotted from a cumulative frequency table.

An ogive or cumulative frequency polygon is a line joining the top right hand corners of the bars in a cumulative frequency graph.

Cumulative frequency

Cumulative frequency is a running total of frequencies.

<table>
<thead>
<tr>
<th>score (x)</th>
<th>tally</th>
<th>frequency (f)</th>
<th>cumulative frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>🌊🌊🌊🌊</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>2</td>
<td>🌊🌊🌊🌊</td>
<td>9</td>
<td>13</td>
</tr>
<tr>
<td>3</td>
<td>🌊🌊🌊</td>
<td>6</td>
<td>19</td>
</tr>
<tr>
<td>4</td>
<td>🌊🌊🌊</td>
<td>7</td>
<td>26</td>
</tr>
<tr>
<td>5</td>
<td>🌊 🌊</td>
<td>3</td>
<td>29</td>
</tr>
<tr>
<td>6</td>
<td>🌊</td>
<td>2</td>
<td>31</td>
</tr>
</tbody>
</table>
Divided bar graph

From: A Maths Dictionary for Kids by Jenny Eather at www.amathsdictionaryforkids.com

A divided bar graph is used for organising and displaying categorical data.

The bar is divided into percentages according to the frequency of items in each category to the total number of items.

Grade 4 - Most Popular Creature

<table>
<thead>
<tr>
<th>Most Popular Creature</th>
<th>Number of Students (frequency)</th>
</tr>
</thead>
<tbody>
<tr>
<td>crabs</td>
<td>10</td>
</tr>
<tr>
<td>dolphins</td>
<td>15</td>
</tr>
<tr>
<td>sharks</td>
<td>20</td>
</tr>
<tr>
<td>turtles</td>
<td>5</td>
</tr>
<tr>
<td>Total</td>
<td>50</td>
</tr>
</tbody>
</table>

1. Convert the frequencies to a percentage.
2. Draw a bar with 10 or 100 divisions.
3. Colour the divisions to match the frequencies.

EXAMPLE: crabs

1. 10/50 x 100 = 20%
2. Bar with 10 divisions.
3. 20% = 2 divisions.

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A histogram is a graph using adjacent rectangles to represent the frequencies of certain ranges or intervals.

A histogram is built from information contained in a frequency distribution table.

**Oceanarium - fish sizes.**

Marine biologists measure the lengths of 30 tagged fish each year to analyse growth patterns.

Each year, the information from a frequency table is used to make a histogram.

<table>
<thead>
<tr>
<th>Fish lengths in centimetres (intervals)</th>
<th>Number of Fish (frequency)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 - 10</td>
<td>4</td>
</tr>
<tr>
<td>11 - 20</td>
<td>9</td>
</tr>
<tr>
<td>21 - 30</td>
<td>8</td>
</tr>
<tr>
<td>31 - 40</td>
<td>5</td>
</tr>
<tr>
<td>41 - 50</td>
<td>4</td>
</tr>
</tbody>
</table>

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A line graph or line chart uses straight lines to join points which represent the data.

Line graphs are often used to show changes in data over a period of time.

Turtle Sightings - Far North Queensland

The sharp decline in turtle numbers seen in 2011 is believed to be a direct result of the devastating Queensland floods and cyclones experienced during the early part of the year.
A picture graph or pictogram uses pictures to represent quantities.

**Pictures may represent one unit ...**

### Oceanarium - Area 2.

<table>
<thead>
<tr>
<th>Type</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>fish</td>
<td><img src="image" alt="Fish pictograms" /></td>
</tr>
<tr>
<td>turtles</td>
<td><img src="image" alt="Turtles pictograms" /></td>
</tr>
<tr>
<td>crabs</td>
<td><img src="image" alt="Crabs pictograms" /></td>
</tr>
<tr>
<td>sharks</td>
<td><img src="image" alt="Sharks pictograms" /></td>
</tr>
</tbody>
</table>

Or a number of units.

- 🐟 = 10
- 🐠 = 5

### Oceanarium - Area 8.

<table>
<thead>
<tr>
<th>Type</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>fish</td>
<td><img src="image" alt="Fish pictograms" /></td>
</tr>
<tr>
<td>turtles</td>
<td><img src="image" alt="Turtles pictograms" /></td>
</tr>
<tr>
<td>crabs</td>
<td><img src="image" alt="Crabs pictograms" /></td>
</tr>
<tr>
<td>sharks</td>
<td><img src="image" alt="Sharks pictograms" /></td>
</tr>
</tbody>
</table>

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A pie graph or pie chart uses a divided circle where each part represents a percentage of the total. Each part is called a sector.

### 3J - Most Popular Marine Creature

<table>
<thead>
<tr>
<th>Most Popular Creature</th>
<th>Number of Students (frequency)</th>
</tr>
</thead>
<tbody>
<tr>
<td>crabs</td>
<td>5</td>
</tr>
<tr>
<td>dolphins</td>
<td>4</td>
</tr>
<tr>
<td>sharks</td>
<td>6</td>
</tr>
<tr>
<td>turtles</td>
<td>3</td>
</tr>
<tr>
<td>seals</td>
<td>2</td>
</tr>
<tr>
<td>Total</td>
<td>20</td>
</tr>
</tbody>
</table>

1. Convert the frequencies to a percentage for the graph labels, e.g. $\frac{5}{20} \times 100 = 25\%$
2. Find the degrees for each sector angle, e.g. $\frac{5}{20} \times 360 = 90^\circ$
3. List the degrees in descending order, e.g. $108^\circ, 90^\circ, 72^\circ, 54^\circ, 36^\circ$
4. Draw a circle and radius. Use a protractor to draw the angles from largest to smallest in a clockwise direction, measuring each next angle from the dividing line of the previous one.
4. Label each sector with the category name and percentage. Write the title.
A scatter plot is a diagram where points are plotted to show the relationship (correlation) between two variables. The points are placed as ordered pairs on a coordinate plane.

**EXAMPLE: Oceanarium Kiosk Management**

To manage ordering supplies more effectively, three scatter plots were made to see if there was any correlation between daily temperatures and sales of ice cream, hamburgers and coffee.

**Positive Correlation**
A positive trend - as one set of values increases, the other set increases.

For example, as the temperature went up, ice cream sales went up.

**Negative Correlation**
A negative trend - as one set of values increases, the other set decreases.

For example, as the temperature went up, hamburger sales went down.

**No Correlation**
No trend - the points are scattered randomly with no visible pattern.

For example, as the temperature went up, there was no apparent effect on coffee sales.

A line of best fit or trend line is a straight line that best represents the values on a scatter plot.
A stem-and-leaf plot is a graph where the values in a set of data are arranged by place value. A stem-and-leaf plot is similar to a histogram but provides more detail because the individual values are shown.

**EXAMPLE: Dolphin sightings - last 12 days.**

A stem-and-leaf plot for the set of data 3, 6, 7, 24, 25, 29, 31, 34, 40, 42, 42, 49

<table>
<thead>
<tr>
<th>stem</th>
<th>leaves</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>3 6 7</td>
</tr>
<tr>
<td>1</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>4 5 9</td>
</tr>
<tr>
<td>3</td>
<td>1 4</td>
</tr>
<tr>
<td>4</td>
<td>0 2 2 9</td>
</tr>
</tbody>
</table>

stems = 10  leaves = 1

If a stem is displayed only once, the leaves are counted as ones. A stem may be displayed 1, 2 or 5 times depending on the data.

Usually the leaf contains the last digit of the number and the stem contains all the other digits.

**To make a stem-and-leaf plot:**

1. Sort the values in ascending order.
2. Draw a vertical line.
3. Determine what place value the stem(s) and leaves will represent.
4. Write the stem values without skipping any numbers.
5. Write the leaf values in order (in a row to the right of each stem value).
6. Add a key and a title.
A step graph is a graph that increases in steps rather than a line.

### Oceanarium - Activity Times

<table>
<thead>
<tr>
<th>Time</th>
<th>Seal Show</th>
<th>Pat Crabs</th>
<th>Dolphin Show</th>
<th>Feed Fish</th>
<th>Shark Show</th>
</tr>
</thead>
<tbody>
<tr>
<td>10:00 am</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>11:00 am</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>12:00 pm</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1:00 pm</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2:00 pm</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

A step graph may display each value as a horizontal line connected to adjacent values by vertical lines.

### Oceanarium Kiosk - Hamburger Prices

<table>
<thead>
<tr>
<th>Year</th>
<th>Price</th>
</tr>
</thead>
<tbody>
<tr>
<td>2006</td>
<td>$1.00</td>
</tr>
<tr>
<td>2007</td>
<td>$2.00</td>
</tr>
<tr>
<td>2008</td>
<td>$3.00</td>
</tr>
<tr>
<td>2009</td>
<td>$4.00</td>
</tr>
<tr>
<td>2010</td>
<td>$5.00</td>
</tr>
<tr>
<td>2011</td>
<td></td>
</tr>
</tbody>
</table>

A step graph can be useful when analysing changes over time.
A travel graph is a line graph showing the relationship between time and distance travelled.

Travel graph of a whale watching cruise.

- Whale watching areas
- Rocky Point
- Wharf

Saturday Cruise

- Moving (travelling)
- Still (stationary)

Steeper = faster
Mean, median, mode

Mean, median and mode are all types of averages.

They are measures used to find the location of the middle (central tendency) of a data set.

**Mean**

The average of all the scores.
Add up all the scores, then divide by the total number of scores.

\[
\begin{align*}
3, & \quad 4, \quad 5, \quad 5, \quad 5, \quad 6, \quad 6, \quad 7, \quad 8, \quad 8, \quad 9 \\
\text{11 scores} & \quad 3 + 4 + 5 + 5 + 5 + 6 + 6 + 7 + 8 + 8 + 9 = 66 \\
& \quad 66 \div 11 = 6 \\
& \quad \text{Mean} = 6
\end{align*}
\]

**Median**

The middle value of an ordered set of scores.
Order the scores from least to greatest.
Locate the middle score.

\[
\begin{align*}
3, & \quad 4, \quad 5, \quad 5, \quad 5, \quad 6, \quad 6, \quad 7, \quad 8, \quad 8, \quad 9 \\
\end{align*}
\]

If the number of scores is even, the median is the average of the two middle scores.

**Mode**

The score that occurs the most.
Order the scores from least to greatest.
Locate the score that occurs the most.

\[
\begin{align*}
3, & \quad 4, \quad 5, \quad 5, \quad 5, \quad 6, \quad 6, \quad 7, \quad 8, \quad 8, \quad 9 \\
\end{align*}
\]

There can be more than one mode. If each score occurs only once there is no mode.
Range

Range is a measure of spread and is the difference between the highest score and the lowest score in a data set.

**Range**

highest score - lowest score = range

| 3, 4, 5, 5, 5, 6, 6, 7, 8, 8, 9 |

9 - 3 = 6

Range = 6

**Range - bar graph.**

Oceanarium - numbers of marine creatures.

- **Reptiles**
- **Molluscs**
- **Crustaceans**
- **Fish**
- **Mammals**

<table>
<thead>
<tr>
<th>100</th>
<th>80</th>
<th>60</th>
<th>40</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

highest score - lowest score = range

100 - 20 = 80

Range = 80

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An outlier is a value far away from most of the other scores in a set of data.

**Outlier in a Dot Plot**

Oceanarium - marine quiz results.

**Considerations**

When calculating averages, outliers may skew a mean so it becomes misleading.

In this case, it may be better to use the median or mode to give a more accurate picture.

Outliers can occur in any data set but it is advisable to check in case an error was made when recording the data.