

Statistics and data types

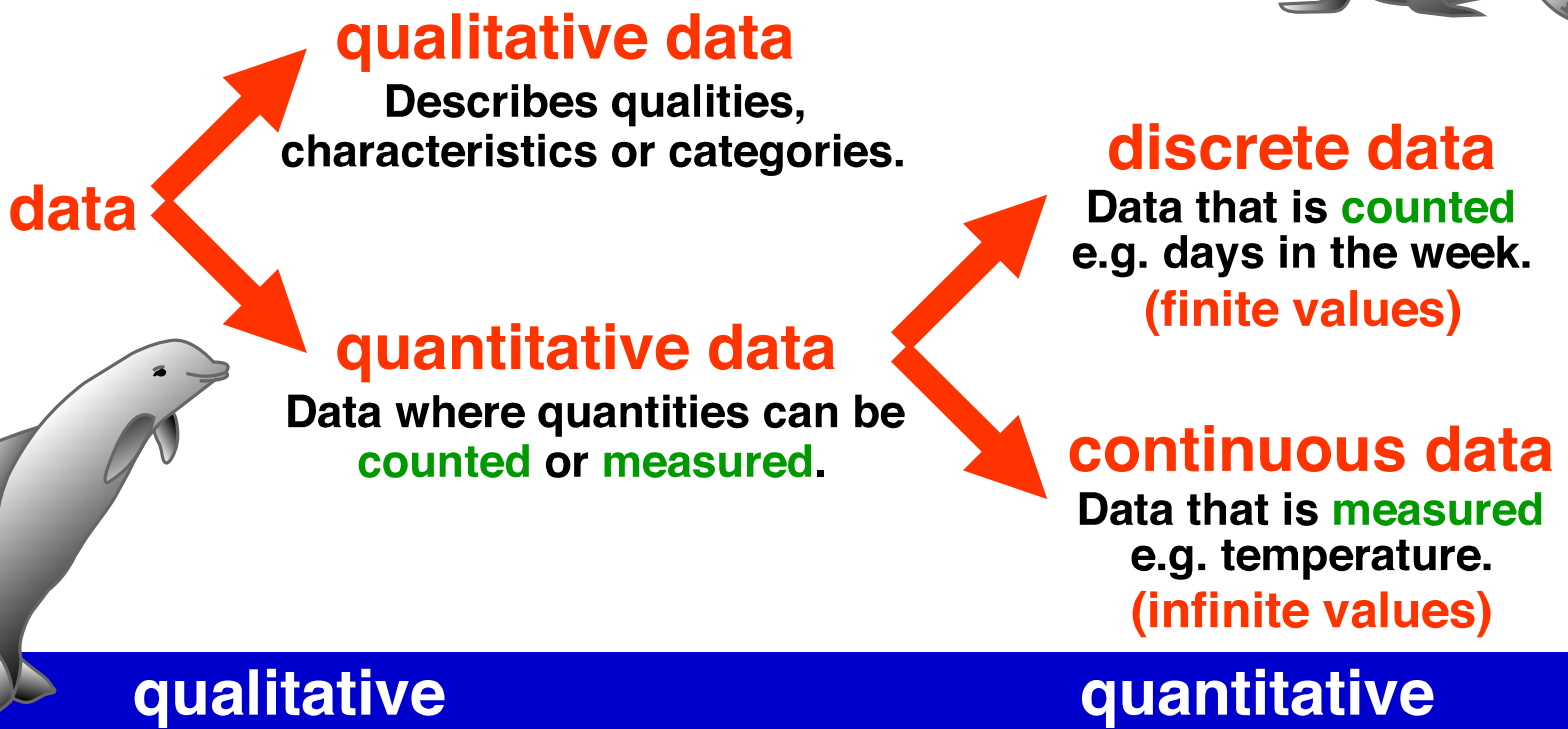
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Statistics is the collection, organisation, presentation, analysis and interpretation of data.

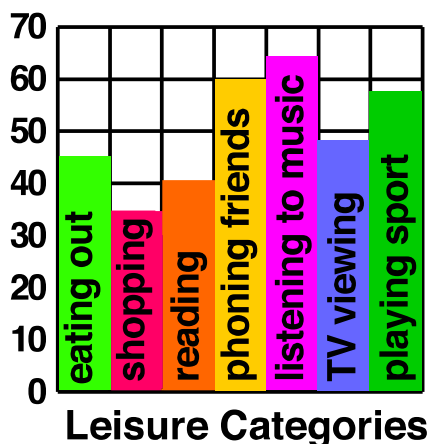
Data is a collection of information which may include facts, numbers, measurements or other information.

Data may be gathered by observation, questioning or measurement and is often organised in graphs or charts for statistical analysis.

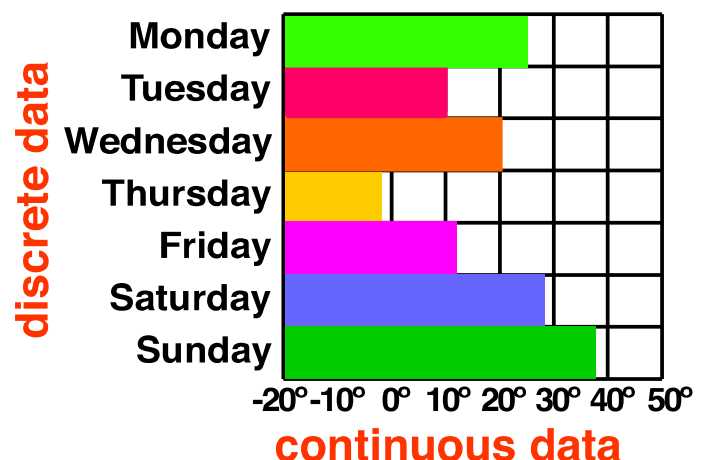
Types of data



Leisure Activities Popularity



Daily Temperature Graph



Population and sample

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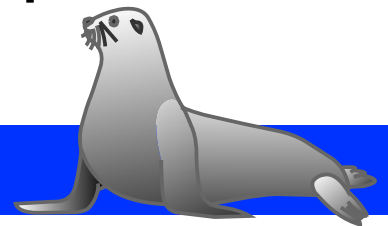
In statistics, the population is the whole set of individuals, items or data from which a statistical sample is drawn.

A sample is a selected part of the population.

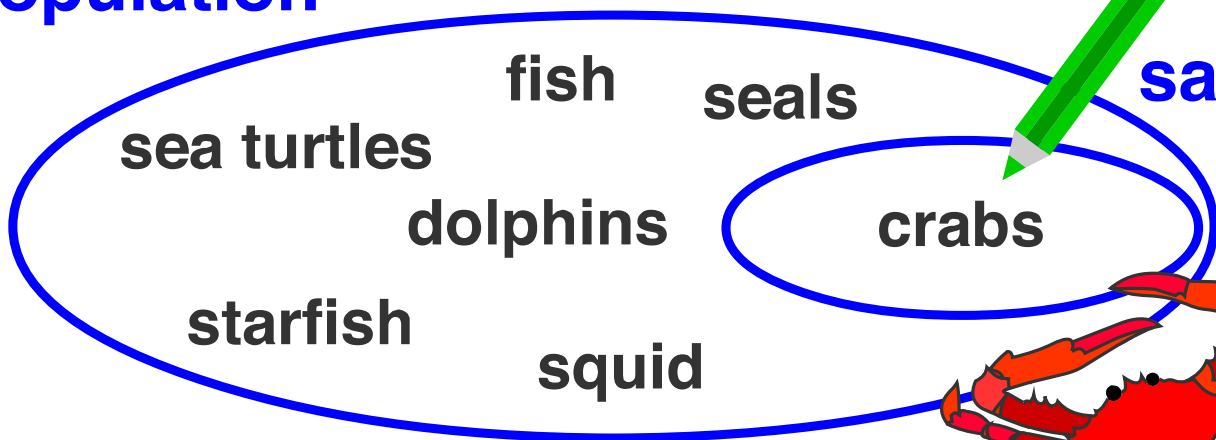
When a population is too big to gather data from, data is collected from a manageable sample instead.



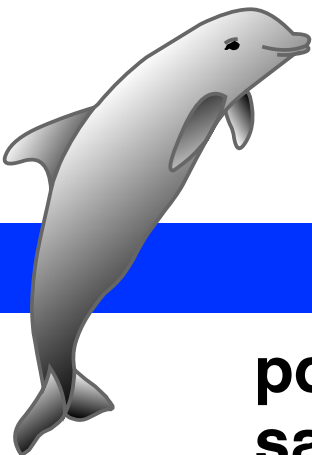
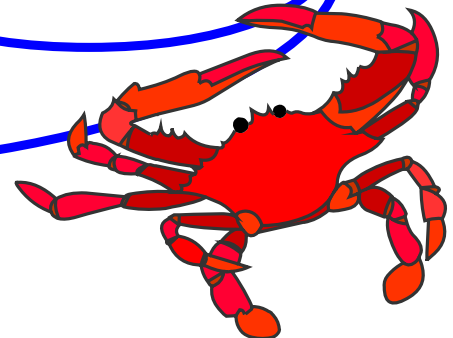
Oceanarium



population



sample



population ... whole group
sample ... part of the group



Tally, score and frequency

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tally

- using marks to record counting.
- count by 5's to get the total 

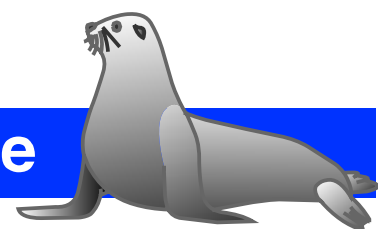
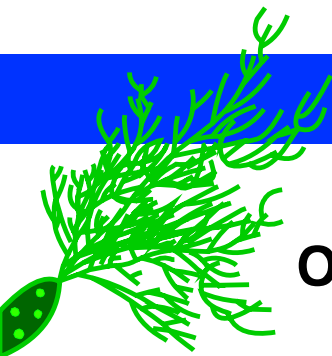
I	1
II	2
III	3
IIII	4
IIII I	5

score

- numerical value.
- any kind of measurement or count.

frequency

- the number of times a particular item appears in a set of data.

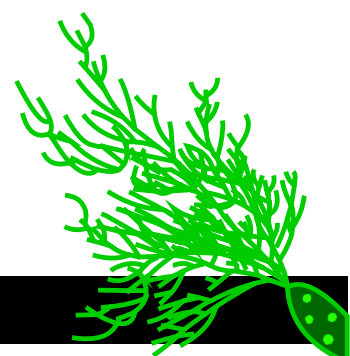
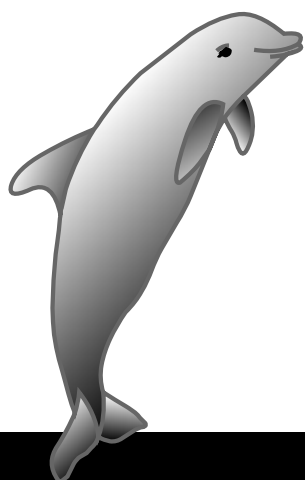


Oceanarium - Frequency Table

A survey was done at schools close to the Oceanarium to see how many classes had been sent to see the exhibits within the last year.

score	tally	frequency (f)
1	IIII	4
2	IIII I	5
3	IIII II	6
4	IIII II II	10
5	III	3
6	II	2

Most schools had a score of 4 class visits.



Number of
class visits

Number of
schools

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Types of graphs

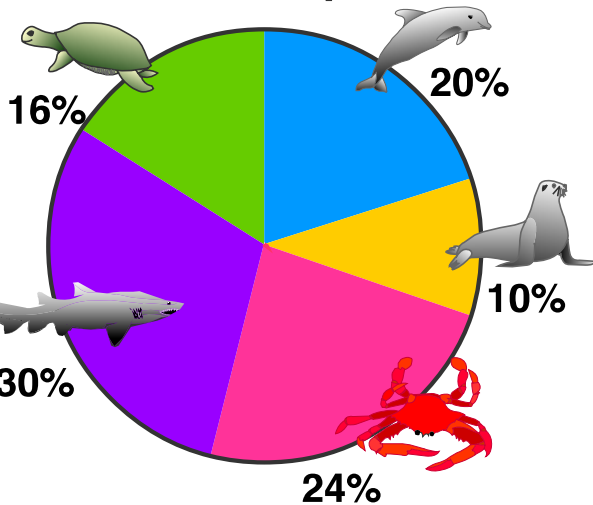
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A graph is a visual diagram used to represent data values.




















There are many types of graphs.

Examples

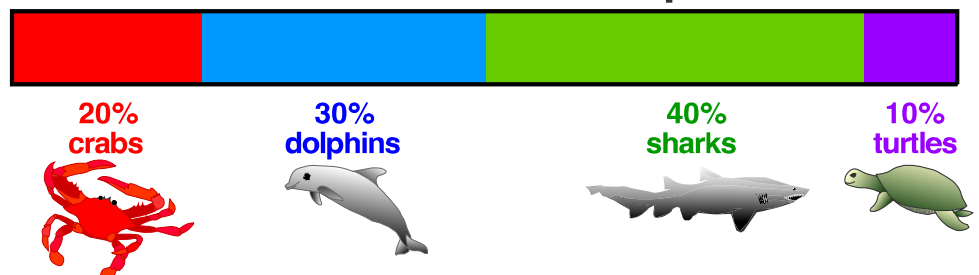
Pie Graph



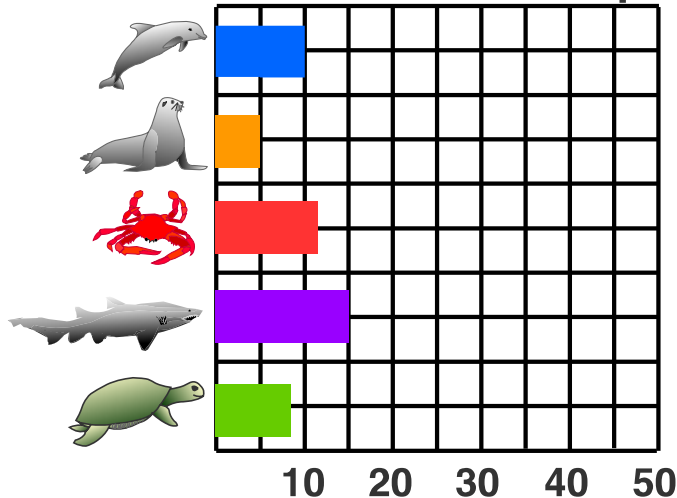
Picture Graph, Pictogram

dolphins	     
seals	    
crabs	     
sharks	 

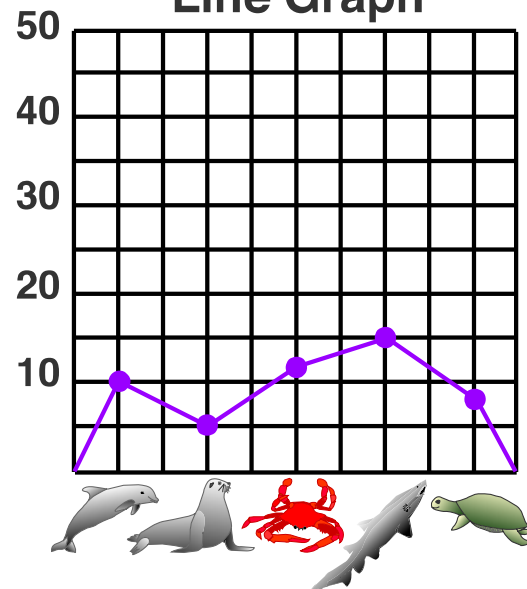
Divided Bar Graph



Horizontal Bar Graph



Line Graph



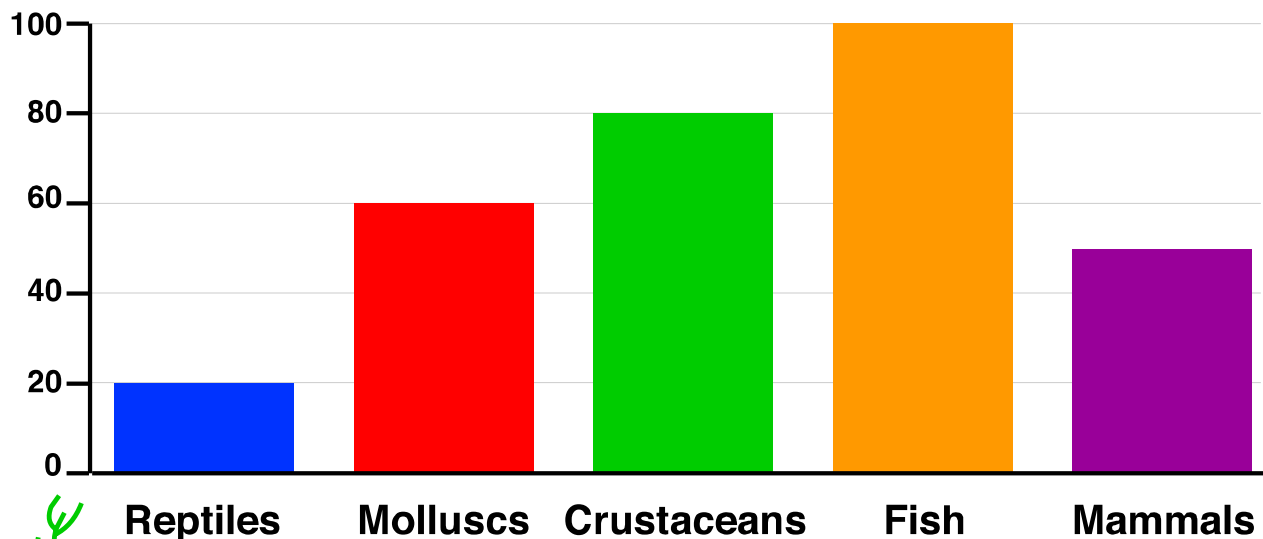
Bar graph, bar chart, column graph

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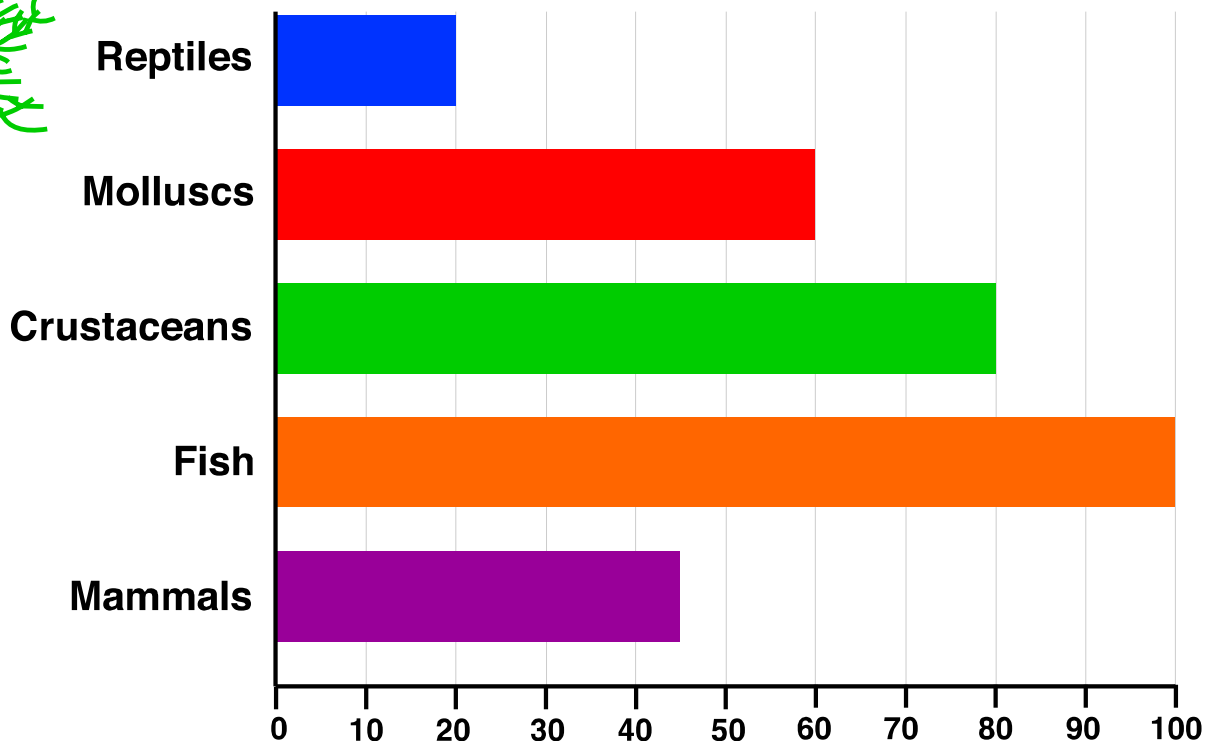
A bar graph or bar chart is a commonly used graph for organising and displaying data.

Bars are used to show quantities or numbers so they can be easily compared.

Oceanarium - numbers of marine creatures.



Bars may be vertical or horizontal.



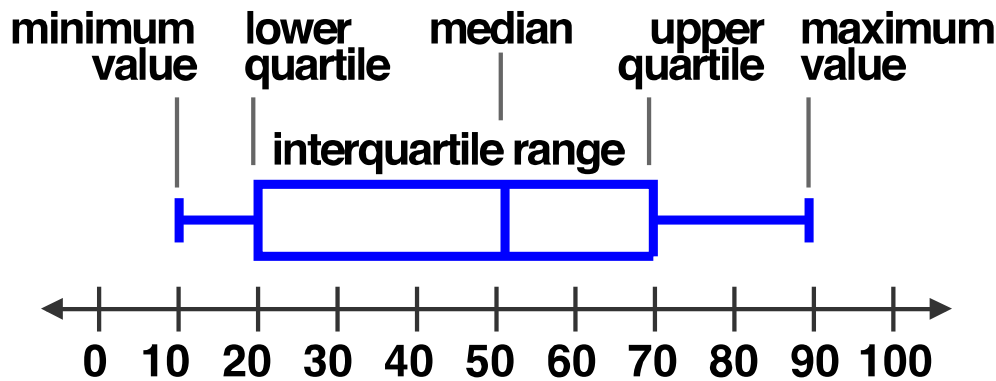
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Box-and-whisker plot, box plot

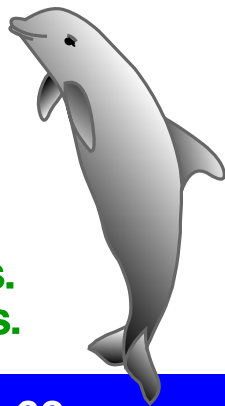
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A box plot is a diagram or graph using a number line to show the distribution of a set of data. It displays the median, upper and lower quartiles, and the maximum and minimum values of the data.



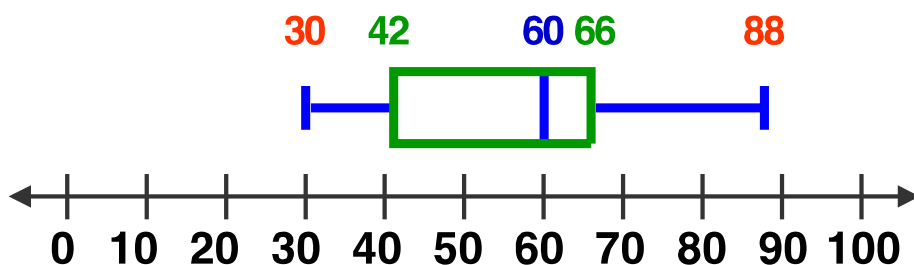
- the box shows the interquartile range.
- a line in the box marks the median.
- the 'whiskers' are lines running from the box to the maximum and minimum values.

- the lower quartile - median of the lower half of the scores.
- the upper quartile - median of the upper half of the scores.



EXAMPLE: 60 60 40 74 63 65 88 41 42 57 30 58 66 66 68

1. Arrange the values in ascending order.
30 40 41 42 57 58 60 60 63 65 66 66 68 74 88
2. Identify the median (the value in the middle).
30 40 41 42 57 58 60 60 63 65 66 66 68 74 88
3. Identify the lower quartile (median of the lower half) and the upper quartile (median of the upper half).
30 40 41 42 57 58 60 60 63 65 66 66 68 74 88
4. Draw a box - from the lower to the upper quartile.
5. Draw a line in the box to show the median.
6. Draw the whiskers - to the minimum and maximum.



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Dot plot

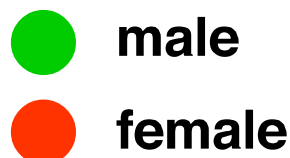
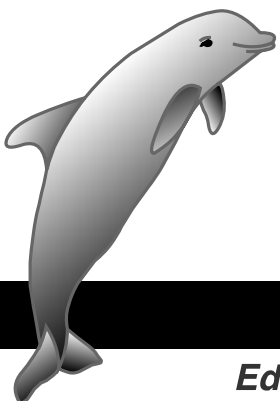
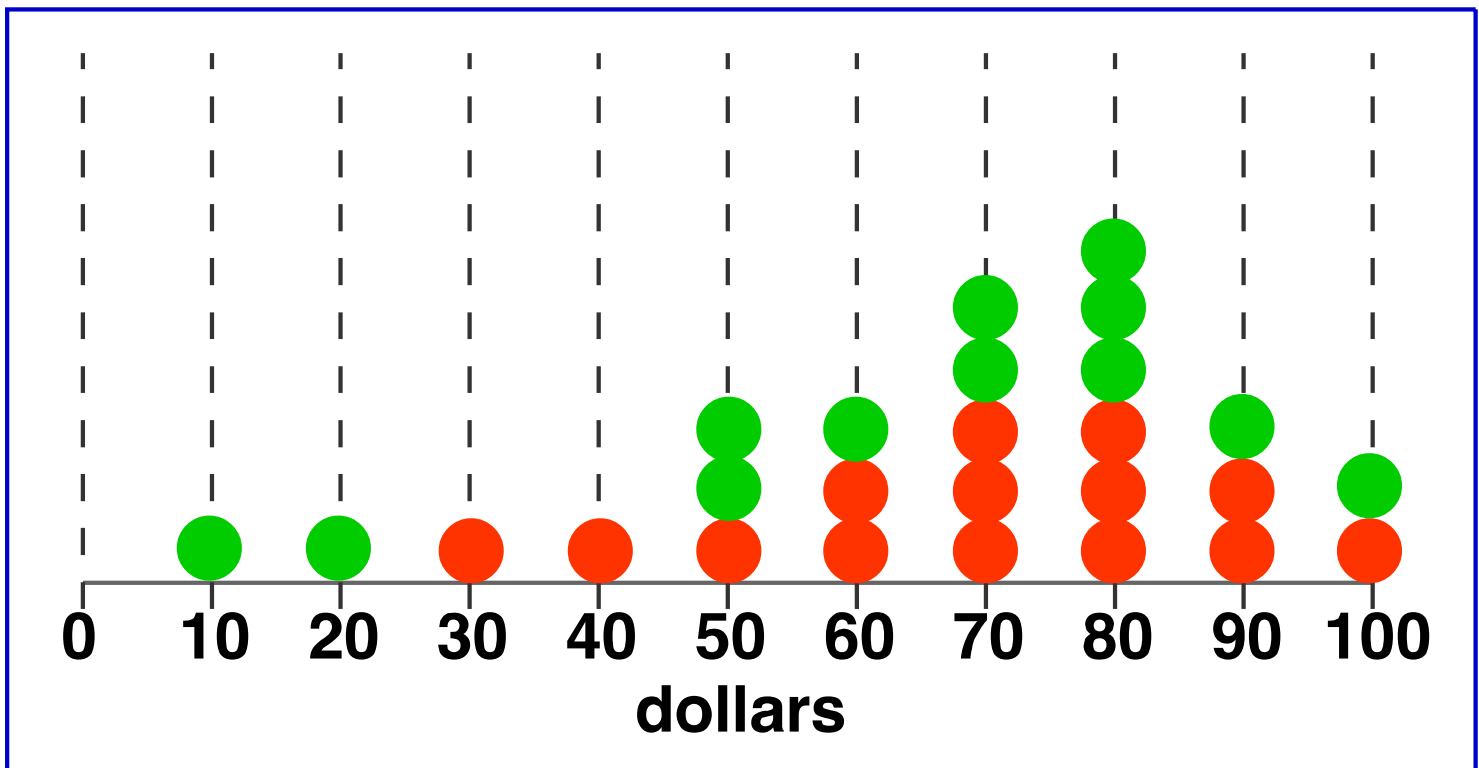
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A dot plot uses a number line long enough to encompass all numbers in the sample, showing a dot over the position corresponding to each number.

If more than one dot falls in the same position, they are stacked up.

A dot plot of spending patterns.

The amount spent by members of a tour group visiting the Oceanarium.

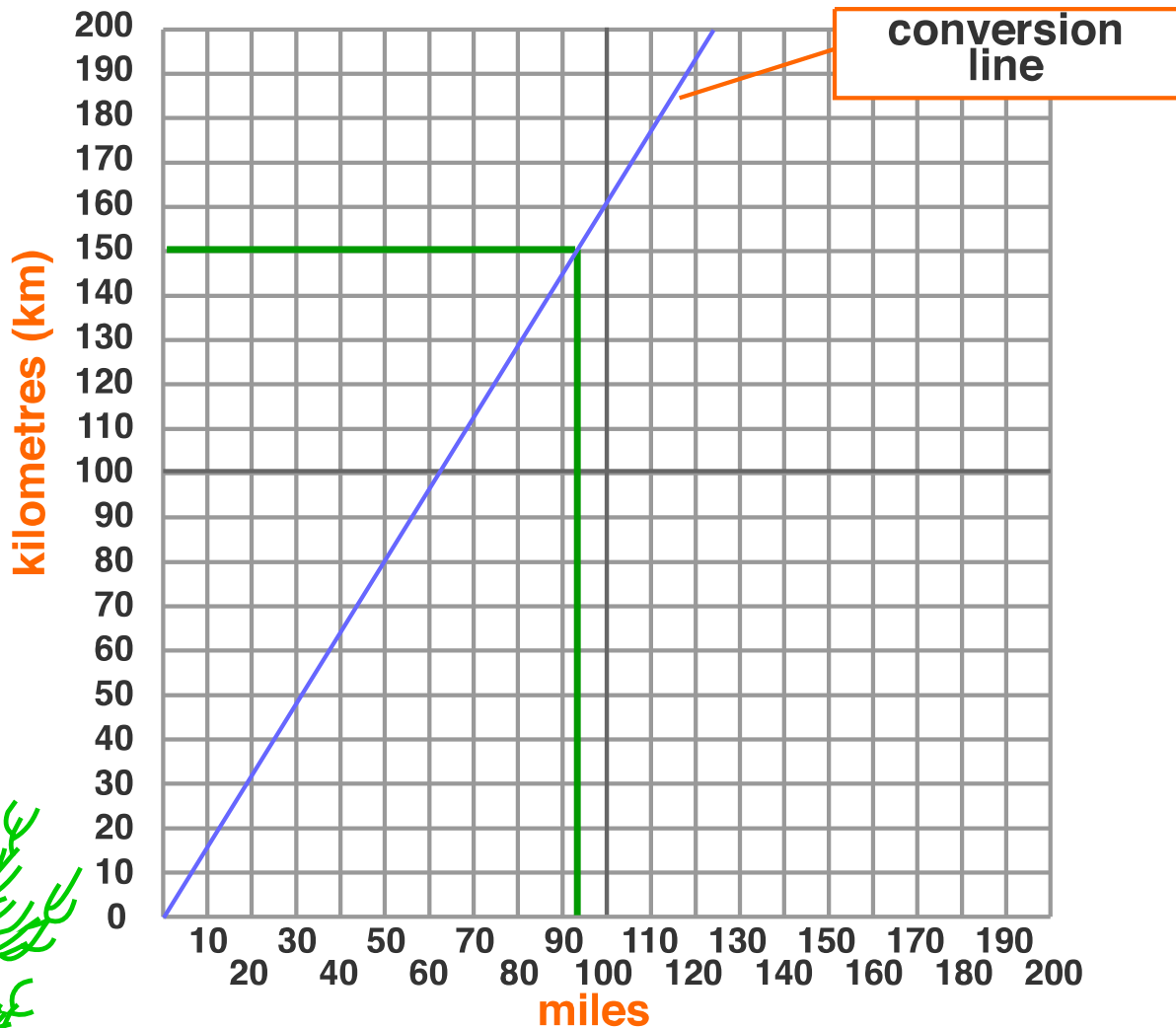


Conversion graph

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A conversion graph is a line graph used to convert one unit to another.

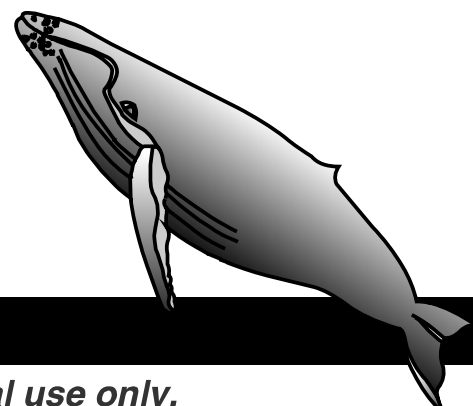
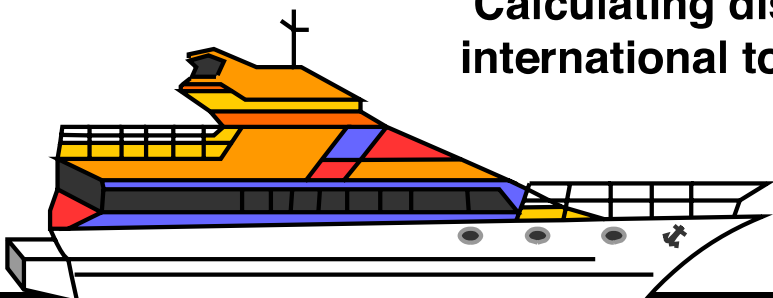
EXAMPLE: kilometres ... miles conversion



Read across and down: 150 km = 93 miles.

Whale Watching

Calculating distances to keep international tourists informed.



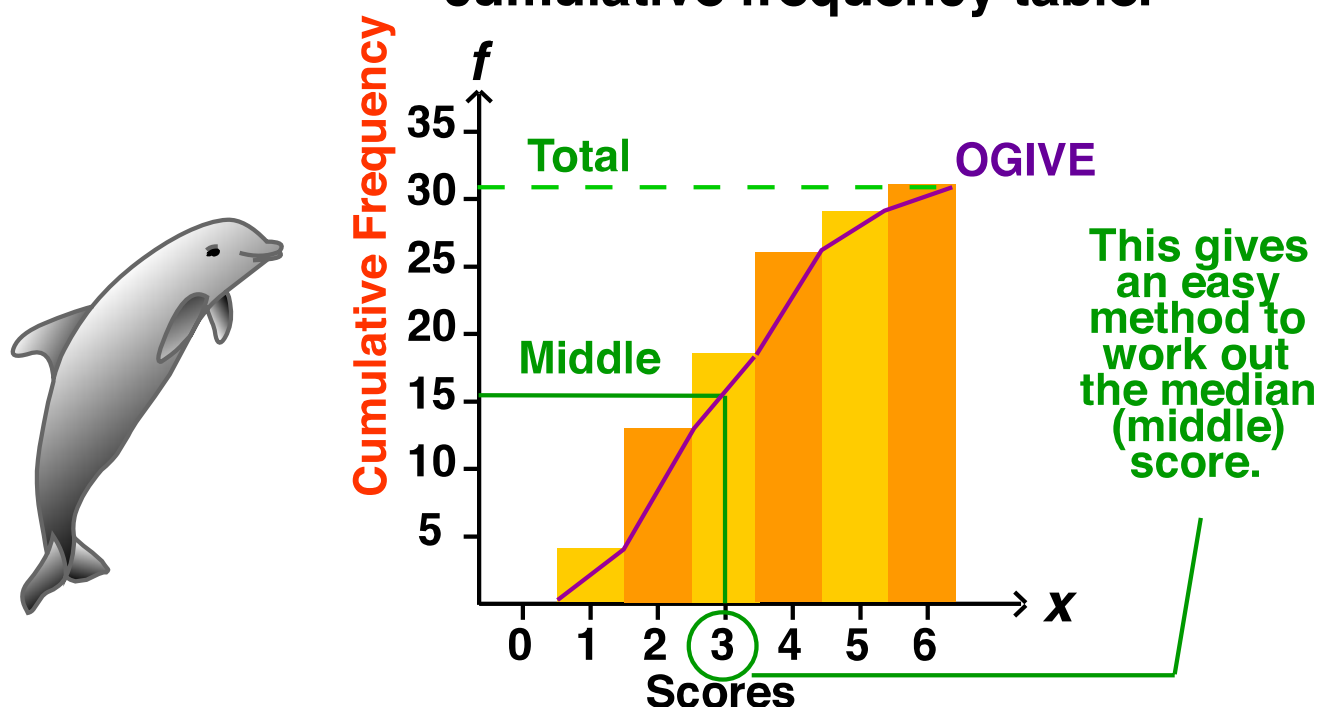
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Cumulative frequency graph

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A cumulative frequency graph is a graph plotted from a cumulative frequency table.



An ogive or cumulative frequency polygon is a line joining the top right hand corners of the bars in a cumulative frequency graph.

Cumulative frequency

Cumulative frequency is a running total of frequencies.

score (x)	tally	frequency (f)	cumulative frequency
1		4	4
2	 	9	13
3	 	6	19
4	 	7	26
5		3	29
6		2	31

Divided bar graph

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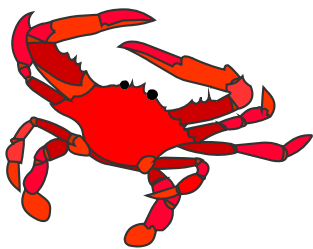
A divided bar graph is used for organising and displaying categorical data.

The bar is divided into percentages according to the frequency of items in each category to the total number of items.

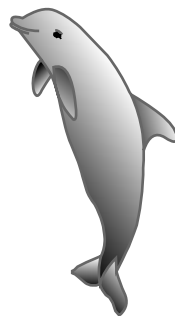
Grade 4 - Most Popular Creature



20%
crabs



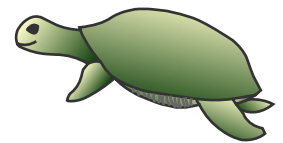
30%
dolphins



40%
sharks



10%
turtles



Making a divided bar graph.

Most Popular Creature	Number of Students (frequency)
crabs	10
dolphins	15
sharks	20
turtles	5

Total 50

1. Convert the frequencies to a percentage.
2. Draw a bar with 10 or 100 divisions.
3. Colour the divisions to match the frequencies.

EXAMPLE: crabs

1. $10/50 \times 100 = 20\%$

2. Bar with 10 divisions.



3. $20\% = 2$ divisions.



Frequency table, histogram

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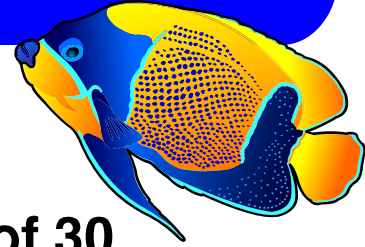
A histogram is a graph using adjacent rectangles to represent the frequencies of certain ranges or intervals.

A histogram is built from information contained in a frequency distribution table.

Oceanarium - fish sizes.

Marine biologists measure the lengths of 30 tagged fish each year to analyse growth patterns.

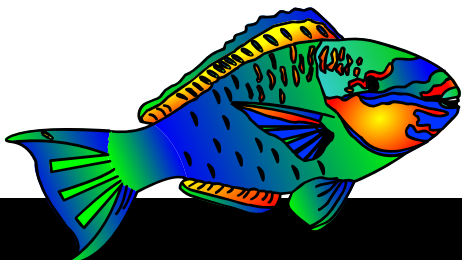
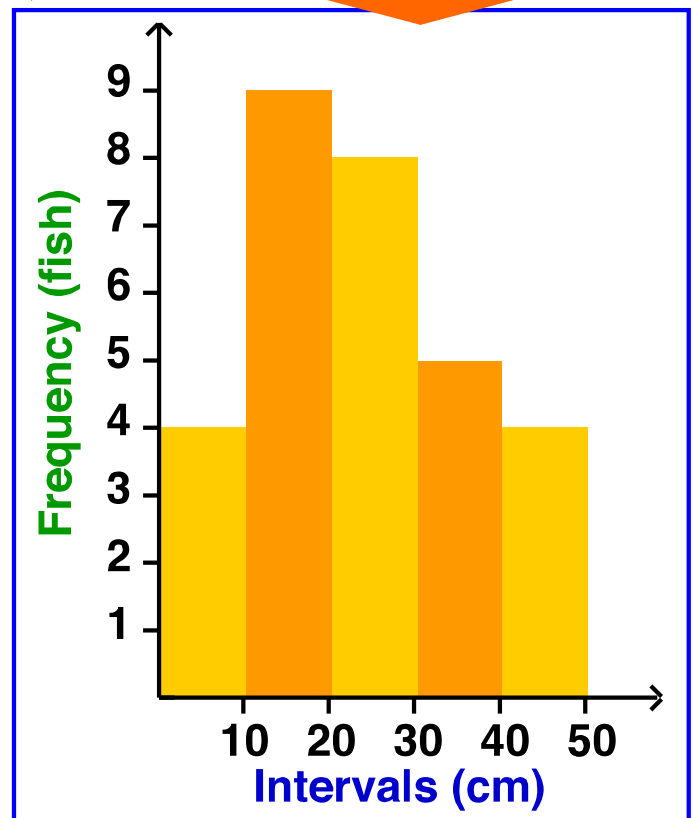
Each year, the information from a frequency table is used to make a histogram.



frequency distribution table

histogram

Fish lengths in centimetres (intervals)	Number of Fish (frequency)
0 - 10	4
11 - 20	9
21 - 30	8
31 - 40	5
41 - 50	4



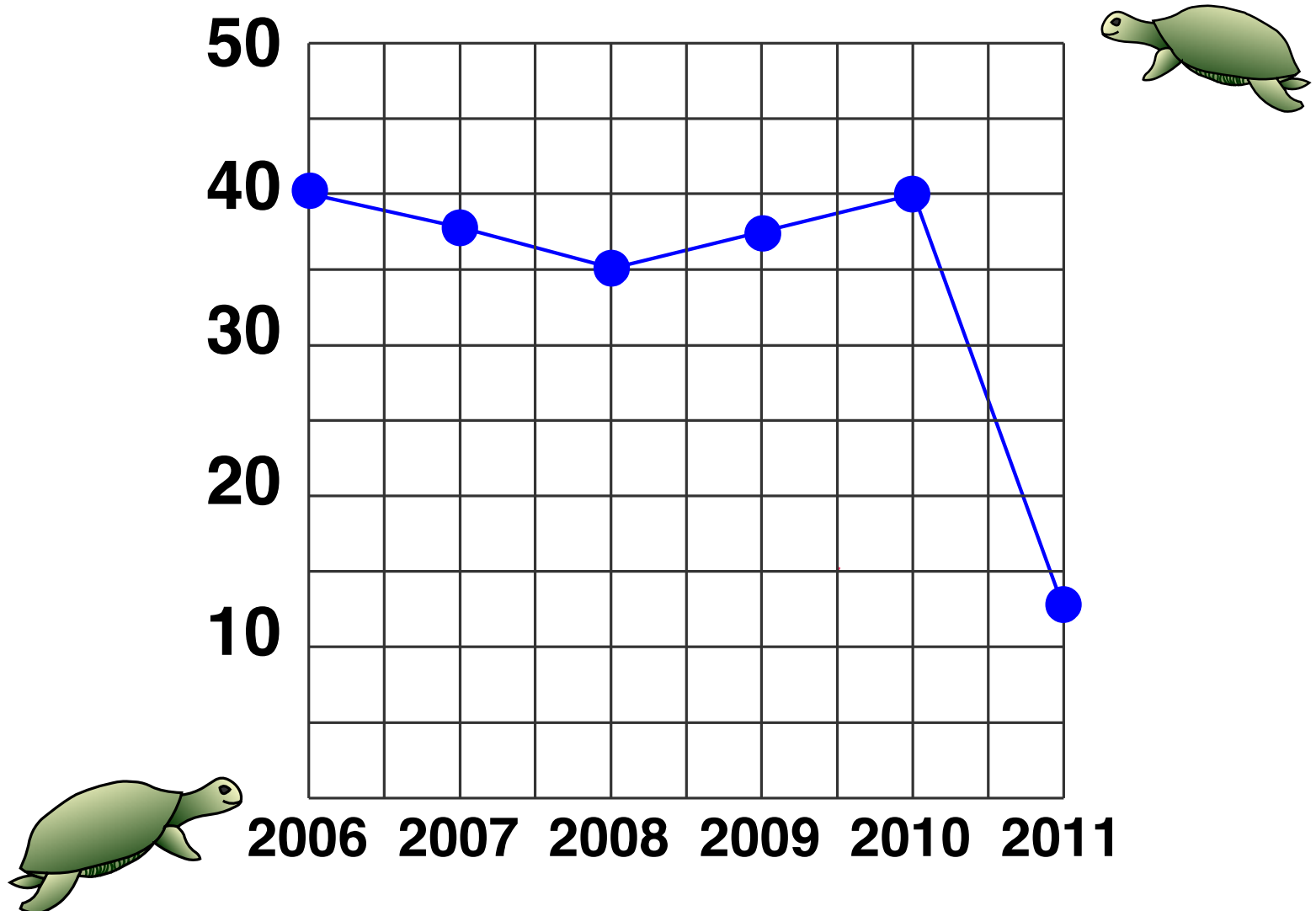
Line graph

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A line graph or line chart uses straight lines to join points which represent the data.

Line graphs are often used to show changes in data over a period of time.

Turtle Sightings - Far North Queensland



The sharp decline in turtle numbers seen in 2011 is believed to be a direct result of the devastating Queensland floods and cyclones experienced during the early part of the year.














Picture graph, pictogram

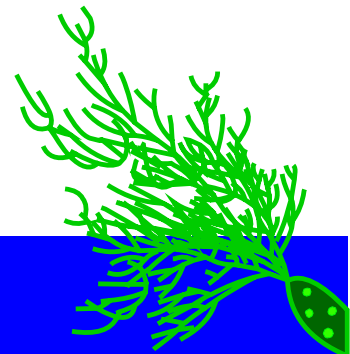
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A picture graph or pictogram uses pictures to represent quantities.

Pictures may represent one unit ...

Oceanarium - Area 2.














Type	Frequency
fish	   
turtles	  
crabs	   
sharks	 

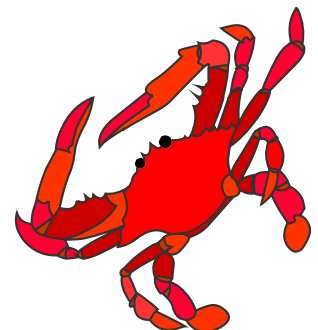


or a number of units.

 = 10  = 5

Oceanarium - Area 8.

Type	Frequency
fish	    
turtles	  
crabs	 
sharks	  



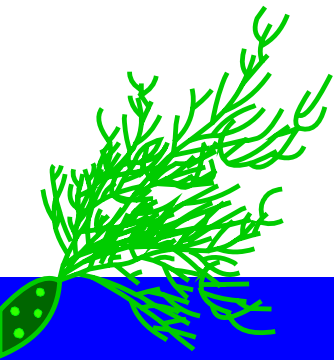
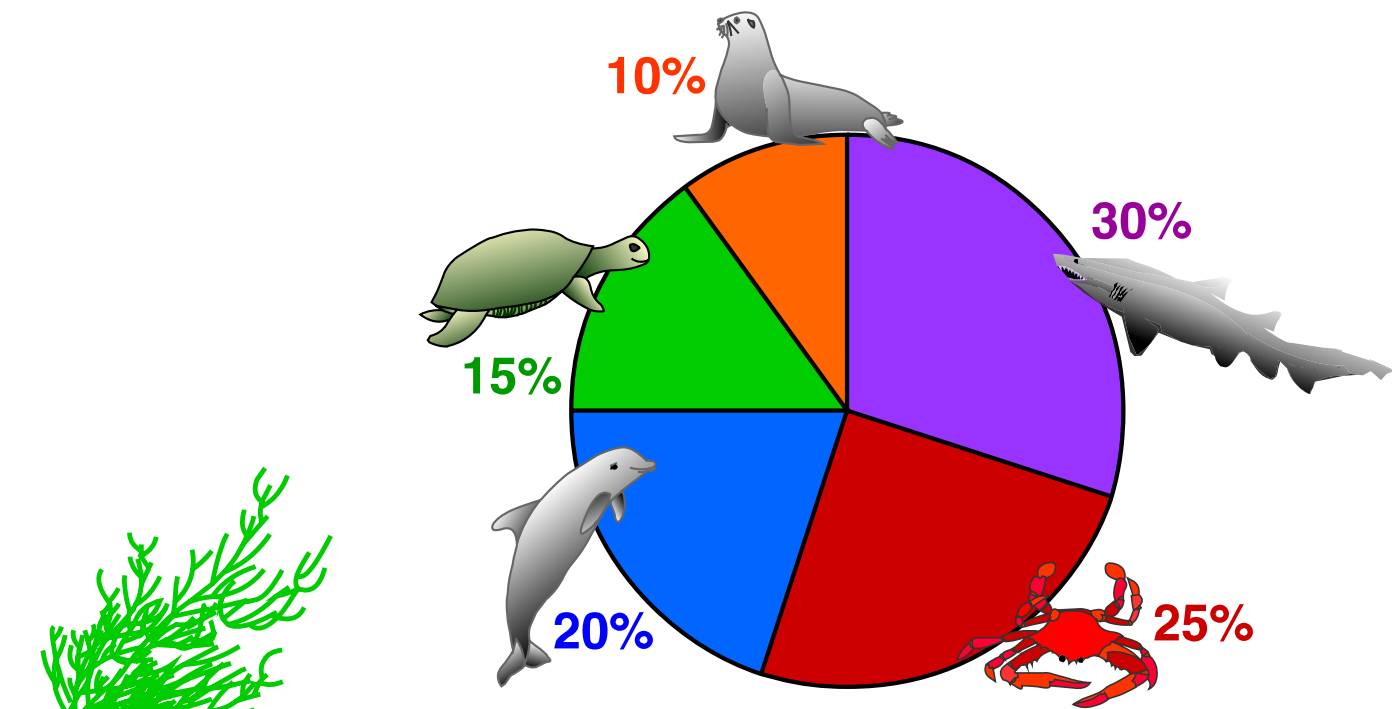
Pie or sector graph, pie chart

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A pie graph or pie chart uses a divided circle where each part represents a percentage of the total.

Each part is called a sector.

3J - Most Popular Marine Creature



Making a pie graph.

Most Popular Creature	Number of Students (frequency)
crabs	5
dolphins	4
sharks	6
turtles	3
seals	2

Total 20

1. Convert the frequencies to a percentage for the graph labels, e.g. $5/20 \times 100 = 25\%$
2. Find the degrees for each sector angle, e.g. $5/20 \times 360 = 90^\circ$
3. List the degrees in descending order, e.g. $108^\circ, 90^\circ, 72^\circ, 54^\circ, 36^\circ$
4. Draw a circle and radius. Use a protractor to draw the angles from largest to smallest in a clockwise direction, measuring each next angle from the dividing line of the previous one.
4. Label each sector with the category name and percentage. Write the title.



Scatter plot or diagram

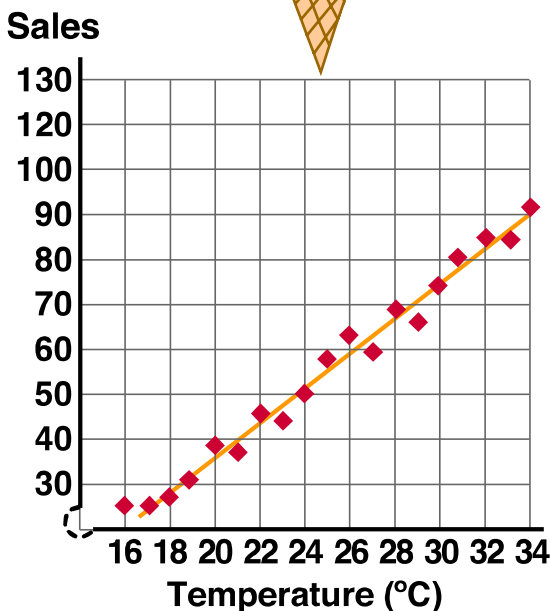
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A scatter plot is a diagram where points are plotted to show the relationship (correlation) between two variables.

The points are placed as ordered pairs on a coordinate plane.

EXAMPLE: Oceanarium Kiosk Management

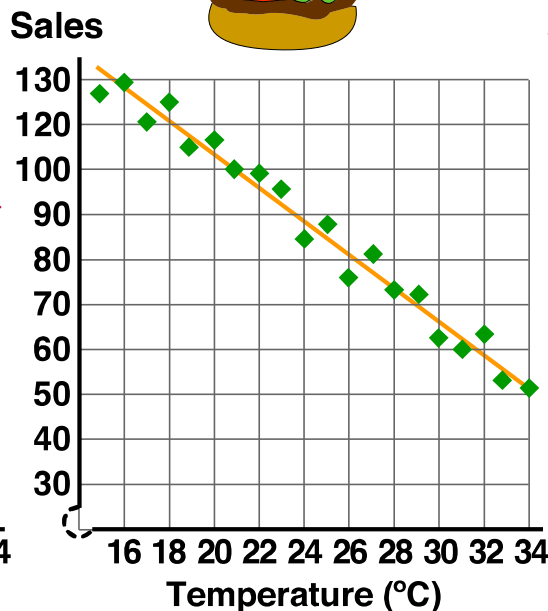
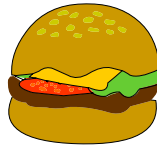
To manage ordering supplies more effectively, three scatter plots were made to see if there was any correlation between daily temperatures and sales of ice cream, hamburgers and coffee.



Positive Correlation

A positive trend - as one set of values increases, the other set increases.

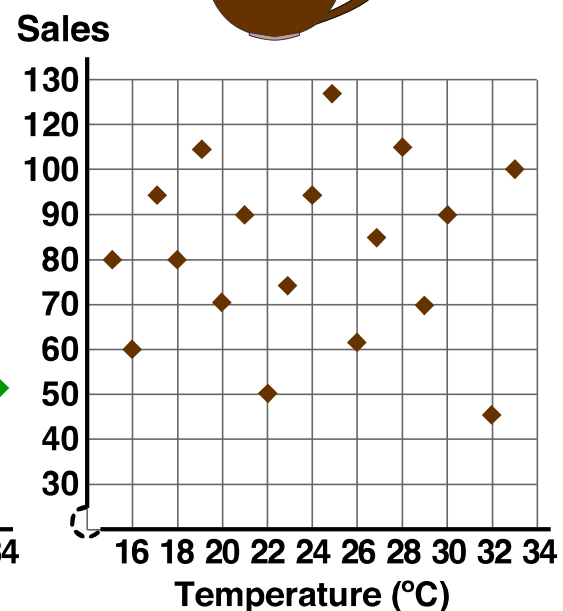
For example, as the temperature went up ice cream sales went up.



Negative Correlation

A negative trend - as one set of values increases, the other set decreases.

For example, as the temperature went up hamburger sales went down.



No Correlation

No trend - the points are scattered randomly with no visible pattern.

For example, as the temperature went up there was no apparent effect on coffee sales.

A line of best fit or trend line is a straight line that best represents the values on a scatter plot.

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Stem-and-leaf plot

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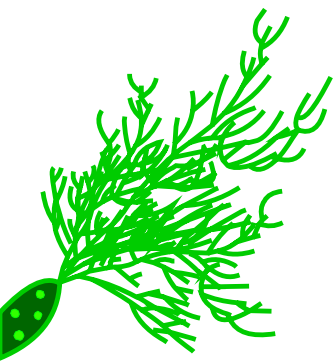
A stem-and-leaf plot is a graph where the values in a set of data are arranged by place value.

A stem-and-leaf plot is similar to a histogram but provides more detail because the individual values are shown.

EXAMPLE: Dolphin sightings - last 12 days.

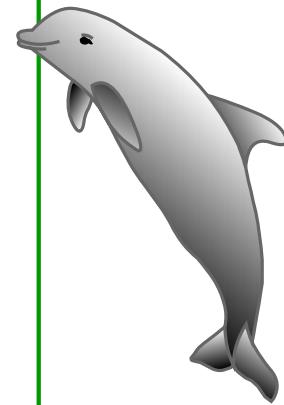
A stem-and-leaf plot for the set of data

3, 6, 7, 24, 25, 29, 31, 34, 40, 42, 42, 49



stem	leaves
0	3 6 7
1	
2	4 5 9
3	1 4
4	0 2 2 9

stems = 10 leaves = 1

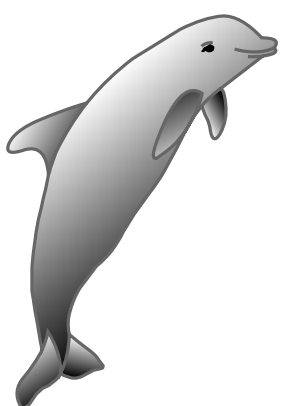
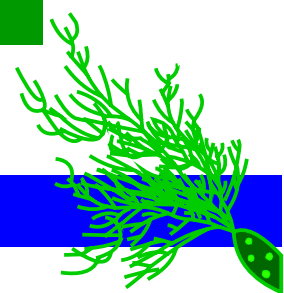


If a stem is displayed only once, the leaves are counted as ones.

A stem may be displayed 1, 2 or 5 times depending on the data.

Usually the leaf contains the last digit of the number and the stem contains all the other digits.

To make a stem-and-leaf plot:

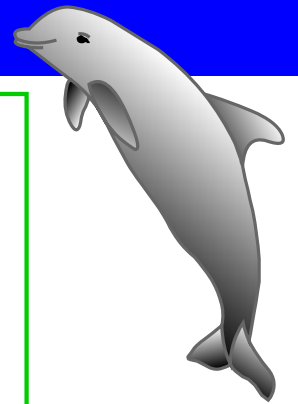
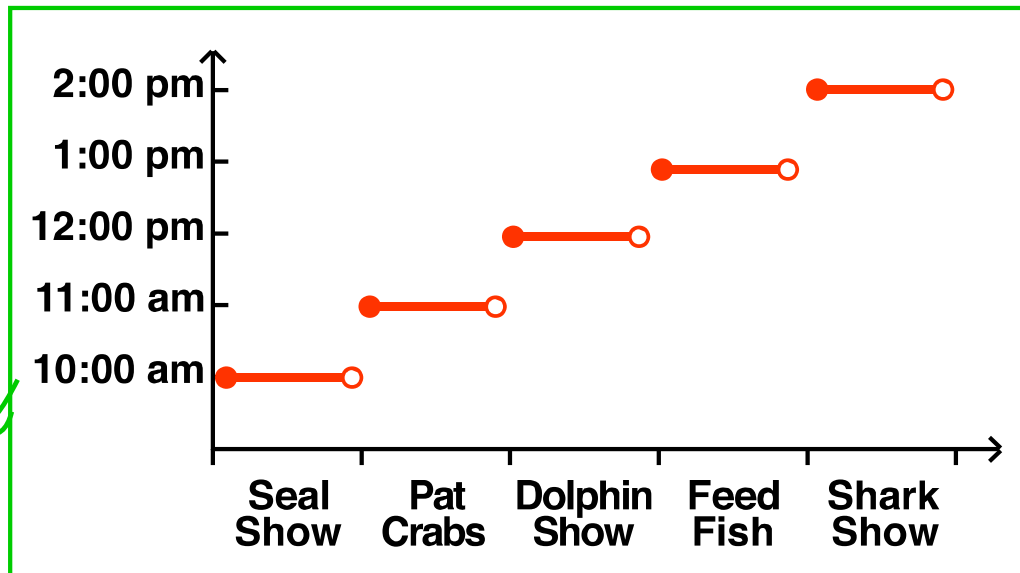
- 
1. Sort the values in ascending order.
 2. Draw a vertical line.
 3. Determine what place value the stem(s) and leaves will represent.
 4. Write the stem values without skipping any numbers.
 5. Write the leaf values in order (in a row to the right of each stem value).
 6. Add a key and a title.
- 

Step graph

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A step graph is a graph that increases in steps rather than a line.

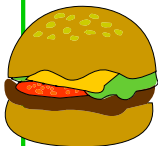
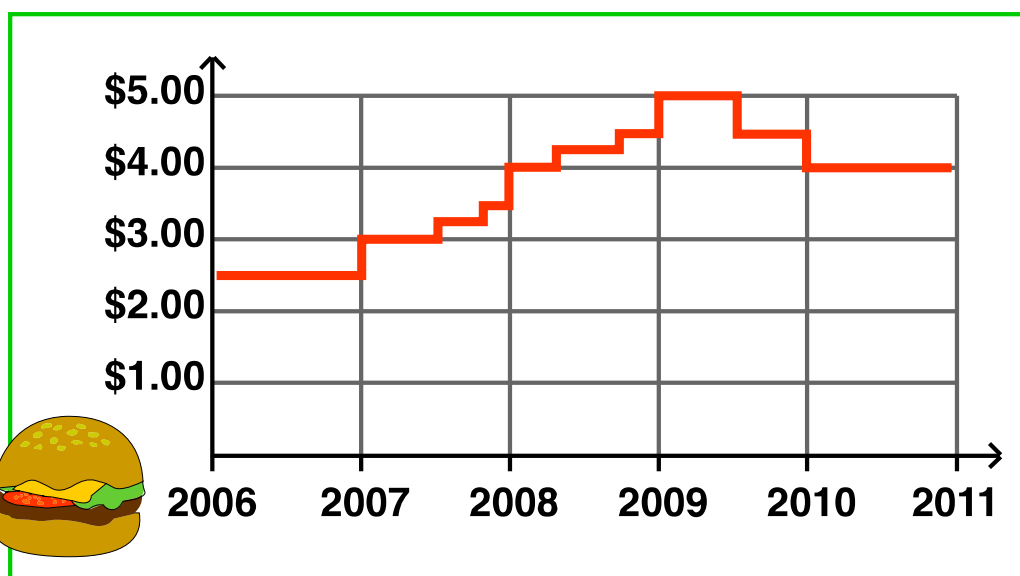
Oceanarium - Activity Times



Start Step Stop

A step graph may display each value as a horizontal line connected to adjacent values by vertical lines.

Oceanarium Kiosk - Hamburger Prices



A step graph can be useful when analysing changes over time.

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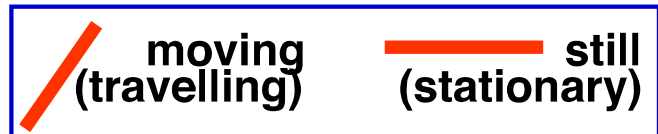
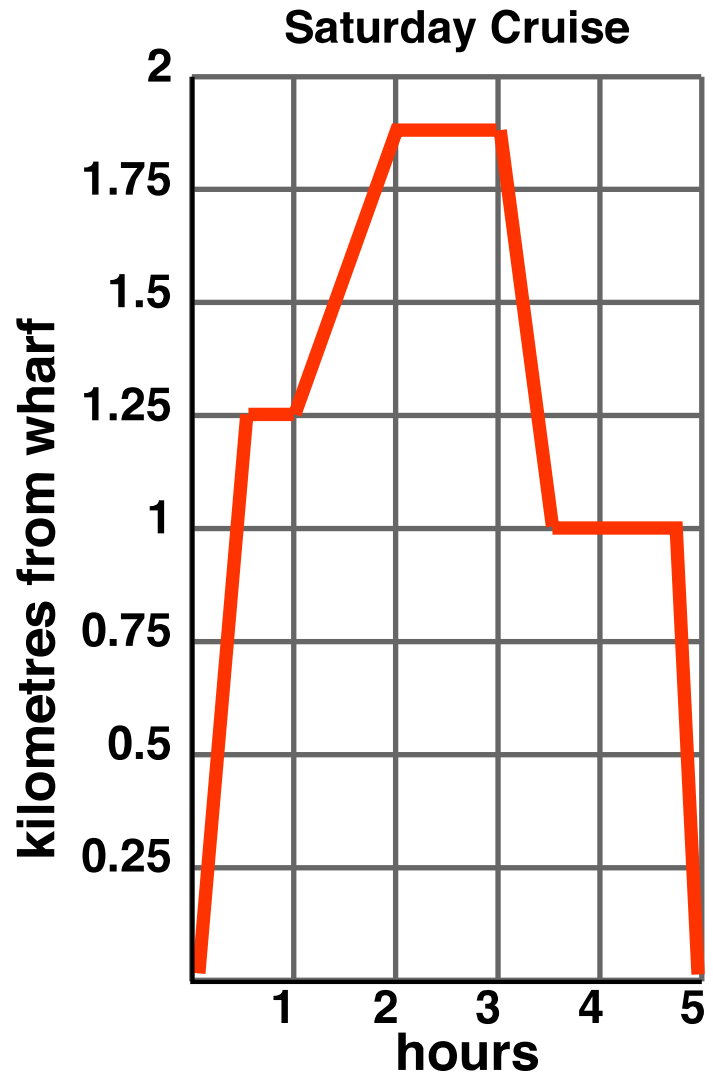
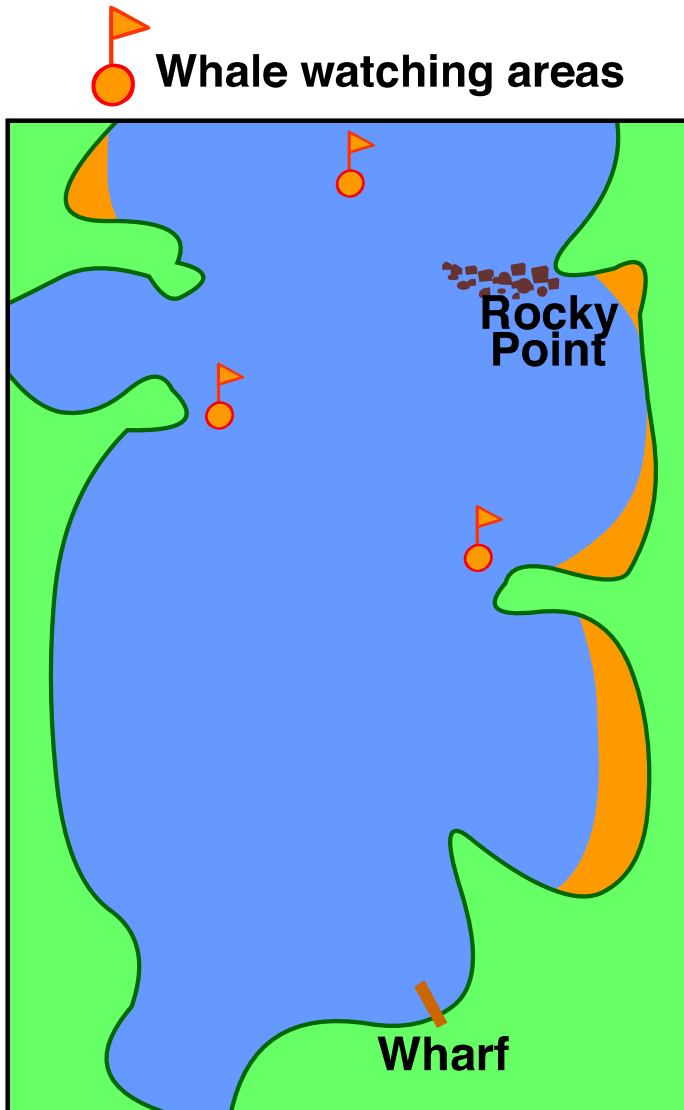
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Travel graph

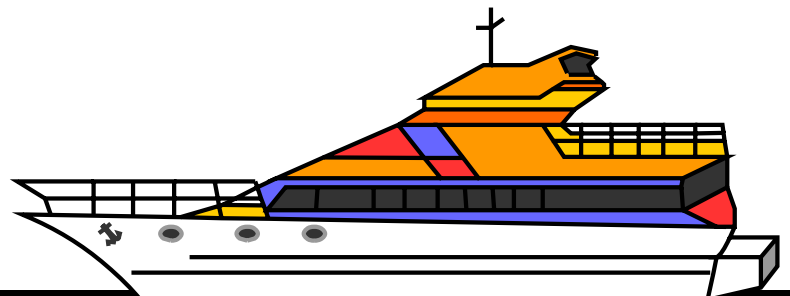
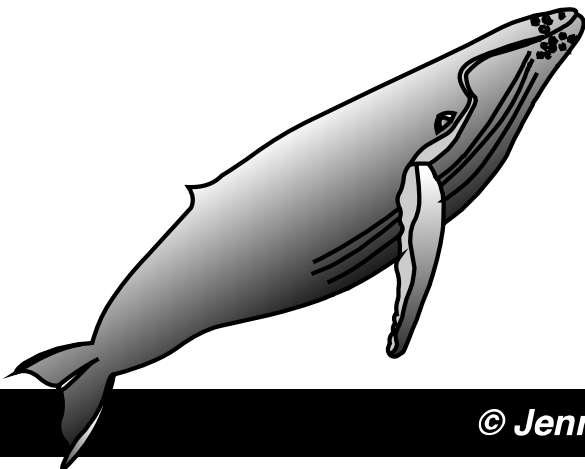
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A travel graph is a line graph showing the relationship between time and distance travelled.

Travel graph of a whale watching cruise.



steeper = faster



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Mean, median, mode

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Mean, median and mode are all types of averages.

They are measures used to find the location of the middle (central tendency) of a data set.

Mean

The average of all the scores.

Add up all the scores, then divide by the total number of scores.

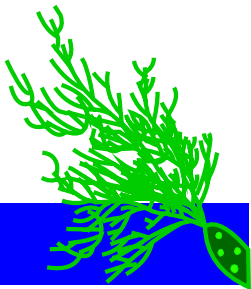
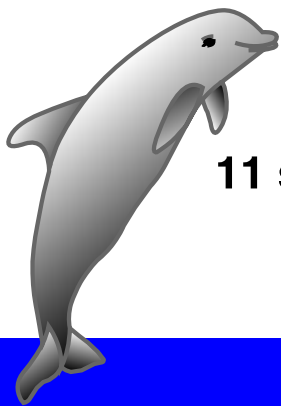
3, 4, 5, 5, 5, 6, 6, 7, 8, 8, 9

11 scores

$$3 + 4 + 5 + 5 + 5 + 6 + 6 + 7 + 8 + 8 + 9 = 66$$

$$66 \div 11 = 6$$

Mean = 6



Median

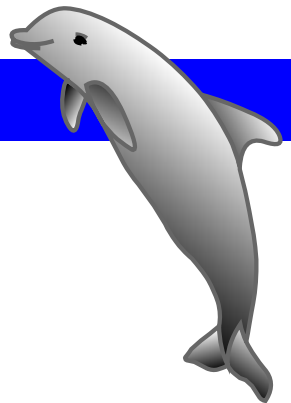
The middle value of an ordered set of scores.

Order the scores from least to greatest.

Locate the middle score.

3, 4, 5, 5, 5, 6, 6, 7, 8, 8, 9

If the number of scores is even, the median is the average of the two middle scores.



Mode

The score that occurs the most.

Order the scores from least to greatest.

Locate the score that occurs the most.

3, 4, 5, 5, 5, 6, 6, 7, 8, 8, 9

There can be more than one mode.

If each score occurs only once there is no mode.

Range

From: A Maths Dictionary for Kids by Jenny Eather at www.amathsdictionaryforkids.com

Range is a measure of spread and is the difference between the highest score and the lowest score in a data set.

Range

highest score - lowest score = range

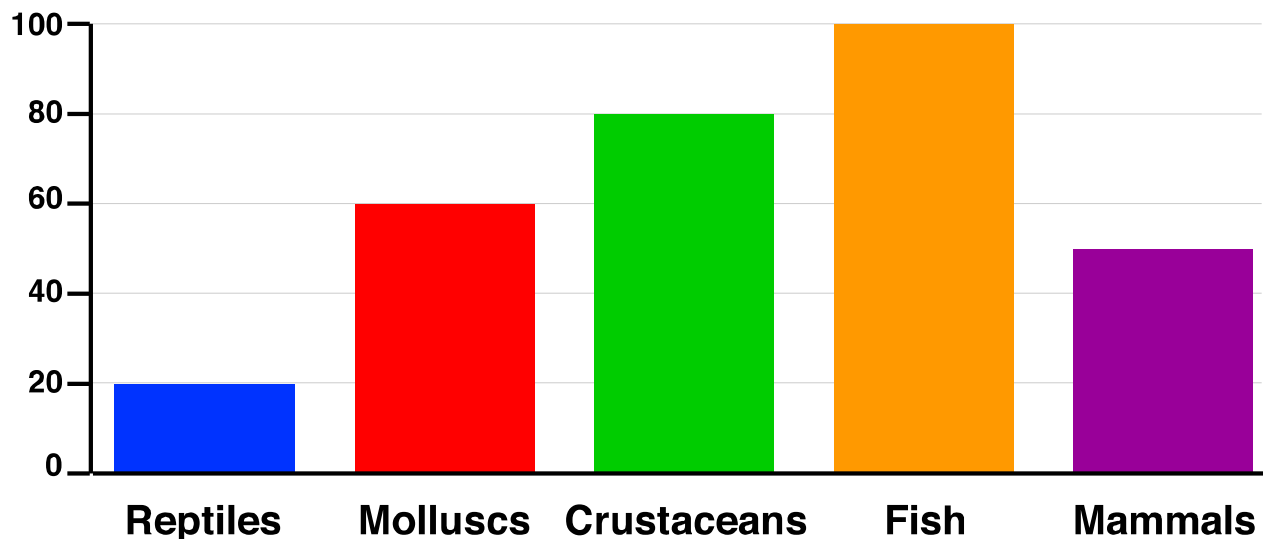
3, 4, 5, 5, 5, 6, 6, 7, 8, 8, 9

$$9 - 3 = 6$$

Range = 6

Range - bar graph.

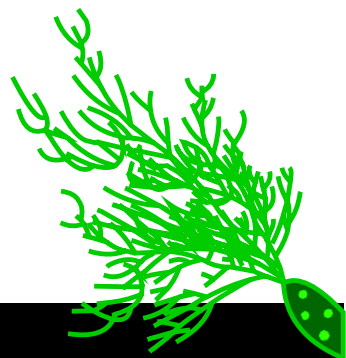
Oceanarium - numbers of marine creatures.



highest score - lowest score = range

$$100 - 20 = 80$$

Range = 80



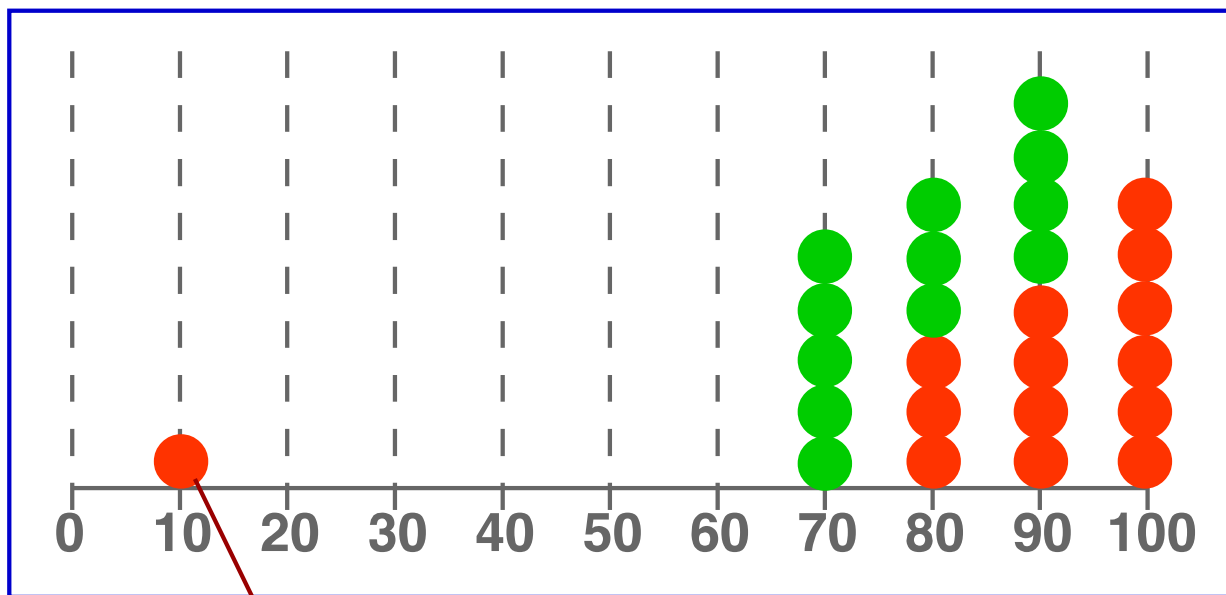
Outlier

From: A Maths Dictionary for Kids by Jenny Eather at www.amathsdictionaryforkids.com

An outlier is a value far away from most of the other scores in a set of data.

Outlier in a Dot Plot

Oceanarium - marine quiz results.



OUTLIER

● male
● female

Considerations

When calculating averages, outliers may skew a mean so it becomes misleading.

In this case, it may be better to use the median or mode to give a more accurate picture.

Outliers can occur in any data set but it is advisable to check in case an error was made when recording the data.